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1. Introduction

- State representation learning aims to infer **low-dimensional** features characterizing states of a dynamical system from high-dimensional data (such as images)
- Learn these features in an unsupervised manner is gaining increasing attention in robotics and reinforcement learning and, for this, latent space models, such as (variational) autoencoders (VAE), are commonly used
- Despite some successful applications, such approaches optimize the reconstruction loss and therefore are based on the following **assumption**: *Similar observations that are close in the image space correspond to similar states of the system*
- We argue that in general, very different images can correspond to the same underlying state when **task-irrelevant** factors of variation are present in the observations. Examples of these factors are changes in the lighting conditions, color changes of the background and camera position

3. Models

- β -VAE**: (Reconstruction loss + KL divergence)

$$\mathcal{L}_{vae}(x) = E_{z \sim q(z|x)} [\log p(x|z)] + \beta \cdot D_{KL}(q(z|x)||p(z))$$
- VAE-A**: (β -VAE loss + contrastive loss)

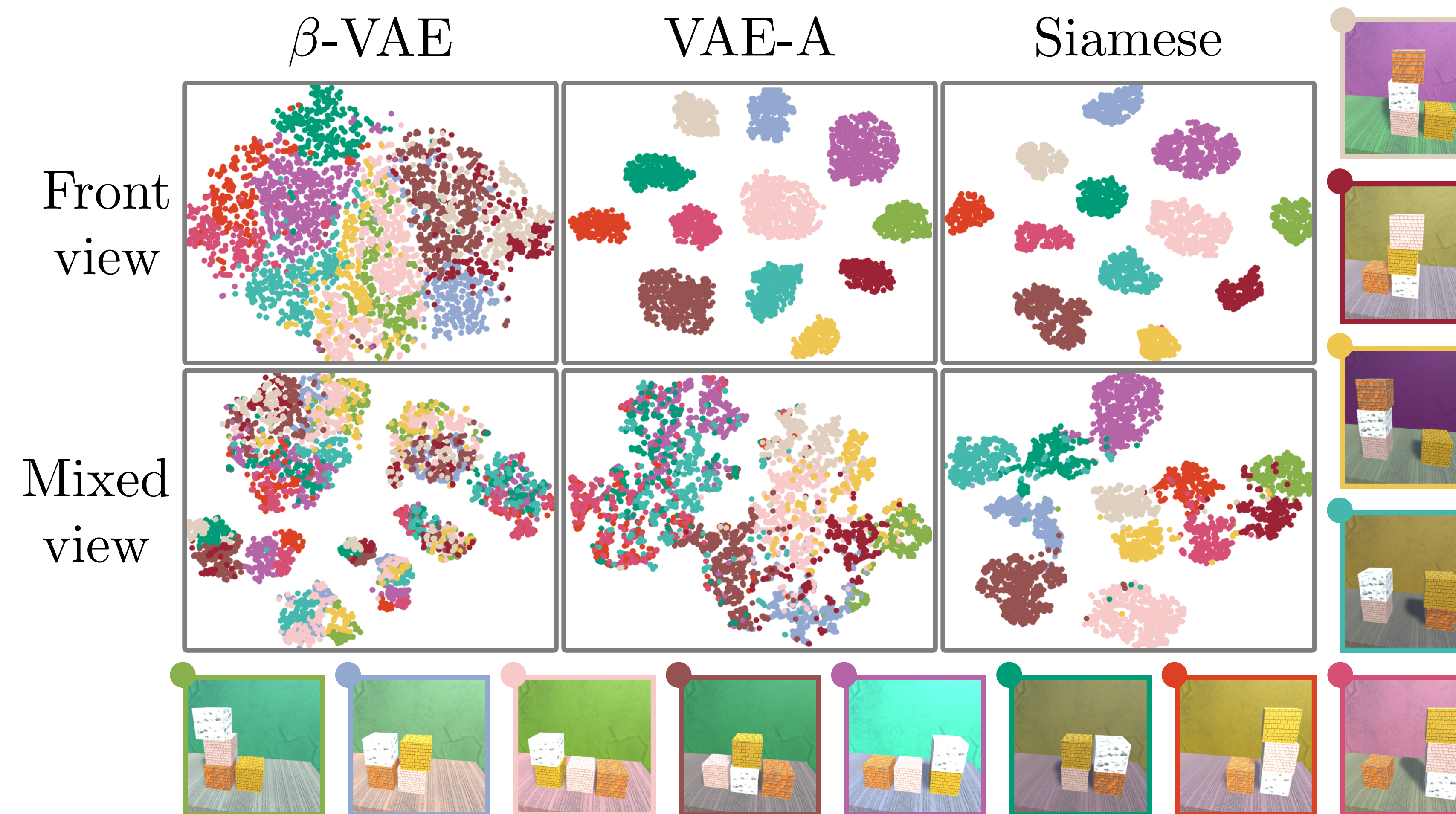
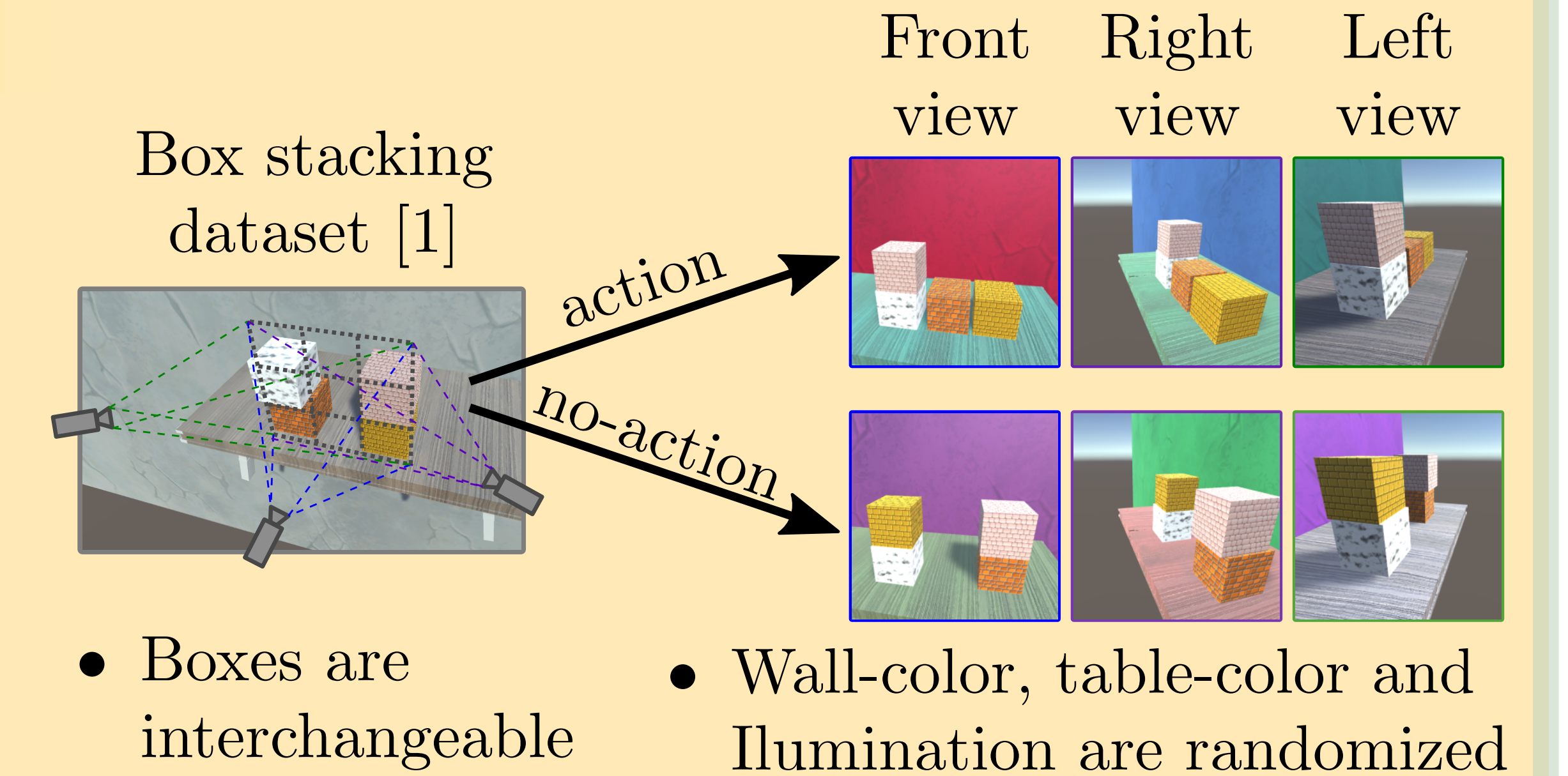
$$\mathcal{L}_{vae-a}(x_i, x_j, a) = \frac{1}{2}(\mathcal{L}_{vae}(x_i) + \mathcal{L}_{vae}(x_j)) + \gamma \mathcal{L}_{action}(x_i, x_j, a)$$

$$\mathcal{L}_{action}(x_i, x_j, a) = \begin{cases} \max(0, d_m - \|z_i - z_j\|_1) & \text{if } a = 1 \\ \|z_i - z_j\|_1 & \text{if } a = 0 \end{cases}$$
- Siamese**: (Contrastive loss)

$$\mathcal{L}_{margin}(x_i, x_j, a) = \frac{1}{2} \begin{cases} \max(0, m - \|z_i - z_j\|_1)^2 & \text{if } a = 1 \\ \|z_i - z_j\|_1^2 & \text{if } a = 0 \end{cases}$$

2. Problem Description and Datasets

- A box stacking task in simulation is used as an example for a robotic manipulation task where the latent representations are built from images
- A dataset \mathcal{D} consists of triplets (I_1, I_2, a) containing an image I_1 , its successor I_2 and a binary variable a denoting if an action took place ($a = 1$) or not ($a = 0$)
- Three viewpoints are used to acquire the images of the scene, based on which four datasets are defined: in $\mathcal{D}_f, \mathcal{D}_r, \mathcal{D}_l$ the images I_1, I_2 are taken from viewpoints "front", "right" and "left" respectively, in \mathcal{D}_m the viewpoints are mixed



4. Results

Models	Dataset \mathcal{D}_f						Dataset \mathcal{D}_m					
	Clust. num.	Clust. hom.	Edges num.	Edge corr.	Paths scores		Clust. num.	Clust. hom.	Edges num.	Edge corr.	Paths scores	
					% all	% any					% all	% any
β -VAE	715	0.98	617	0.95	8.05	8.3	757	0.95	644	0.93	1.0	1.0
VAE-A	12	1.0	24	1.0	100.0	100.0	87	0.86	91	0.85	17.89	20.3
Siamese	12	1.0	25	0.96	94.21	98.1	25	0.95	64	0.88	49.47	52.6
Oracle	12	1.0	24	1.0	100.0	100.0	12	1.0	24	1.0	100.0	100.0

5. Discussion

- \mathcal{D}_f fulfills the assumption that changes in the observations significantly correlate with changes in the system states
- β -VAE generates a fragmented latent space for both datasets (high number of clusters), achieving poor planning performance [1]
- VAE-A achieves perfect performance with dataset \mathcal{D}_f , as reconstruction loss is beneficial in this case, while a drop is recorded with \mathcal{D}_m
- Siamese achieves very good results with \mathcal{D}_f and best performance with \mathcal{D}_m
- We conclude that:

(i) performance improvement is achieved with weak supervision

(ii) VAE-based encodings may be poorly structured when task-irrelevant factors of variation are present in the dataset

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